

EECE 370 Formula Sheet:

Chapter 1:

$$H = \frac{N \cdot i}{lc} [A/m] \quad \mu_0 = 4\pi \cdot 10^{-7} \quad \lambda = N \cdot \phi [Wb \cdot t] \quad \text{Power factor correction:}$$

$$mmf = N \cdot i = \phi \cdot R_t \quad \phi = B \cdot A [Wb] \quad L = \frac{\lambda}{i} [Wb \cdot t/A] \quad P = VI \cos(\theta) [W]$$

$$B = \mu \cdot H [T] \quad \mu = \mu_0 \cdot \mu_r \quad w = \frac{1}{2} Li^2 \quad Q = VI \sin(\theta) [VAR]$$

$$R = \frac{l_c}{\mu \cdot A} \quad F = i \cdot (B \times l) = i \cdot l \cdot B \quad E = (V \times B) \cdot l = B \cdot l \cdot v \quad S = VI [VA]$$

Laws:

Ampere's:  $N \cdot i = \sum H \cdot l$  Faraday's:  $e = N \cdot \frac{d\phi}{dt}$  Lenz's:  $e = -N \cdot \frac{d\phi}{dt}$

3-Phase Circuits:

Parameter \ Connection	Y-Connected	$\Delta$ -Connected
Current	$I_l = I_\phi$	$I_l = \sqrt{3} I_\phi$
Voltage	$V_l = \sqrt{3} V_\phi$	$V_l = V_\phi$
Real Power	$3V_\phi I_\phi \cos(\theta)$ or $\sqrt{3} V_l I_l \cos(\theta)$	$3V_\phi I_\phi \cos(\theta)$ or $\sqrt{3} V_l I_l \cos(\theta)$
Reactive Power	$3V_\phi I_\phi \sin(\theta)$ or $\sqrt{3} V_l I_l \sin(\theta)$	$3V_\phi I_\phi \sin(\theta)$ or $\sqrt{3} V_l I_l \sin(\theta)$
Apparent Power	$S = \sqrt{p^2 + q^2}$	$S = \sqrt{p^2 + q^2}$

Chapter 2: Transformers:

$$E_{max} = \omega \cdot N \cdot \phi_{max} \quad E_{rms} = 4.44 \cdot f \cdot N \cdot \phi_{max} \quad \phi_{max} = \sqrt{2} \phi_{rms}$$

$$e_{max} = \sqrt{2} e_{rms}$$

Ideal Transformers:

$$\frac{V_p}{V_s} = \frac{N_p}{N_s} = \alpha \quad \frac{I_p}{I_s} = \frac{N_s}{N_p} = \frac{1}{\alpha} \quad \frac{Z_p}{Z_s} = \left(\frac{N_p}{N_s}\right)^2 = \alpha^2$$

Real Transformers: (same equations as above)

$$E_p = V_p - I_p(R_p + jX_p) \quad E_s = V_s + (R_s + jX_s) I_s \quad I_p = I_\phi + I_s'$$

Quality Parameters:

$$\text{efficiency: } \eta = \frac{P_{out}}{P_{in}} * 100 = \frac{P_{out}}{P_{out} + P_{loss}} * 100 = 1 - \frac{P_{loss}}{P_{in}} * 100 [\%]$$

$$P_{loss} = I_p^2 R_p + I_s^2 R_s + I_c^2 R_c \quad \text{Copper loss: } = I_s'^2 * R_{eq} \quad \text{Core Loss} = \frac{V_p^2}{R_c}$$

$$\text{Voltage Regulation: } \frac{V_{snl} - V_{sfl}}{V_{sfl}} * 100$$

Transformer testing:

$$\text{OC-Test: } S_{oc} = V_{oc} * I_{oc} \quad R_c = \frac{V_{oc}^2}{P_{oc}} \quad Q_{oc} = \sqrt{S_{oc}^2 - P_{oc}^2} \quad X_m = \frac{V_{oc}^2}{Q_{oc}}$$

$$\text{SC-Test: } R_{eq} = \frac{P_{sc}}{I_{sc}^2} \quad Z_{eq} = \frac{V_{sc}}{I_{sc}} \quad X_{eq} = \sqrt{Z_{eq}^2 - R_{eq}^2} \quad R_p = R'_s = 0.5 R_{eq} \quad X_{lp} = X'_{ls} = 0.5 * X_{eq}$$

Autotransformers:

$$\frac{V_l}{V_h} = \frac{N_c}{N_c + N_{se}} \quad \frac{I_l}{I_h} = \frac{N_{se} + N_c}{N_c} \quad S_{in} = V_l * I_l \quad S_{out} = V_h * I_h \quad \frac{S_{fo}}{S_w} = 1 + \frac{N_c}{N_{se}}$$

Phase Transformers:

$$Y-\Delta: \frac{V_{lp}}{V_{ls}} = \sqrt{3} \alpha \quad \Delta-Y: \frac{V_{lp}}{V_{ls}} = \frac{\alpha}{\sqrt{3}} \quad \Delta-\Delta: \frac{V_{lp}}{V_{ls}} = \alpha$$

AC Machinery Fundamentals

$$e = 2B l v \sin(\theta) \quad \theta = \omega t \quad v = r \omega \quad A = 2r l \quad e_{rms} = 4.44 f N_c \phi_{max} \quad SR = \frac{S_{nl} - S_{fl}}{S_{fl}}$$

$$mmf_p = 1.5 * mmf_m \cos(\theta - \omega t) \quad \theta_{el} = \frac{p}{2} \theta_{mech} \quad n = \frac{120f}{p} \quad \omega = \frac{2\pi n}{60} \quad \tau = 2r l B \sin(\omega t)$$

$$e(t) = \sqrt{2} E_{rms} \sin(\omega t) \quad E_a = \frac{N_c}{\sqrt{2}} \phi \omega \quad P_{out} = 3V_\phi \frac{E_a \sin(\delta)}{X_s} = T_{ind} \omega_n$$

Testing:

$$\text{DC: } R_a = \frac{V_{dc}}{2I_{dc}} \quad Z_s = \frac{V_{oc}}{I_f} \quad X_s = \sqrt{Z_s^2 - R_a^2}$$

Induction motors:

$$\text{Slip: } S = \frac{n_s - n_m}{n_s} * 100 [\%] \quad n_m = 120 \frac{f}{p} (1 - s)$$

$$P_{scl} = 3I_1^2 R_1 \quad P_{rct} = 3I_2^2 R_2 \quad P_g = 3I_2^2 \left(\frac{R_2}{s}\right) \quad P_{conv} = P_g (1 - s) \quad T_{ind} = \frac{P_g}{\omega_s} \quad T_l = \frac{P_{out}}{\omega_m}$$